



**E1262 Jan 2015, 2016, 2017 3:0**

## **Selected Topics in Markov Chains and Optimization**

### **Instructor**

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### **Teaching Assistant**

None

Email: None

**Department: Electronic Systems Engg.**

Course Time: Tu., Th., 11:30 to 1 pm.

Lecture venue: Old conf. room

Detailed Course Page: None

### **Announcements**

None

### **Brief description of the course**

To introduce graduate level students advanced topics in Markov chains, graphs and combinatorics, and optimization.

### **Prerequisites**

Graduate level stochastic processes and basic optimization theory.

### **Syllabus**

Finite state Markov Chains: Rate of convergence to steady state, Eigenstructure of the transition matrix, Perron-Frobenius Theorem, Reversible transition matrices, bounds on convergence rates; Markov Chain Monte Carlo: Knapsack problem – Target distribution sampler, Gibbs sampling, Metropolis-Hastings algorithm, Simulated Annealing, Examples from Bayesian networks and inference problems; Topics in Graph Theory: Matchings and Factors with applications, Connectivity and Paths; Enumeration combinatorics: Generating functions, Sieve methods, Posets; Semidefinite Programming: Quadratically Constrained Quadratic Programming (QCQP), Maximum Eigenvalue and Matrix Norm minimization, Applications to combinatorial problems

## **Course outcomes**

Students will get a flavor of fairly advanced topics in Markov chains, graph theory, combinatorics and optimization useful to their research, build upon existing theory towards applications. In some cases, research papers are directly discussed.

## **Grading policy**

Homeworks: 30%

Mid Term: 20%

Final exam: 50%

## **Assignments**

Exercise problems from books and some research papers.

## **Resources**

Norris J.R., Markov Chains, Cambridge University Press, ISBN-10: 0521633966.

Hajek Bruce, An Exploration of Random Processes for Engineers (course notes for EC-534, "Random Processes"), <http://www.ifp.illinois.edu/~hajek/>

Bremaud Pierre, Markov Chains: Gibbs Fields, Monte Carlo Simulation and Queues, Springer, 1999

West Douglas, Introduction to Graph Theory, Pearson 2nd ed., ISBN-10: 0130144002.

Vandenberghe L. and Boyd S., Semidefinite Programming, in SIAM Review, March 1996